

Assignment 5, Part 1, Specification

SFWR ENG 2AA4

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The purpose of this software design exercise is to design, specify, implement and test a module for storing the state of an Othello game. The game board is represented as a two dimensional sequence, with the first dimension the row and the second dimension the column. The indexes are relative to the upper left hand corner of the board; that is, row 0 and column 0 are at the top left.

Othello Module

Module

Othello

Uses

N/A

Syntax

Exported Constants

SIZE = 8 *//size of the board in each direction*

Exported Types

cellT = { FREE, BLACK, WHITE }

Exported Access Programs

| Routine name | In | Out | Exceptions |
|-------------------|-------------------------|---------|--|
| init | | | |
| move | integer, integer, cellT | | OutOfBoundsException, InvalidMoveException, WrongPlayerException |
| switch_turn | | | ValidMoveExistsException |
| getb | integer, integer | cellT | OutOfBoundsException |
| get_turn | | cellT | |
| count | cellT | integer | |
| is_valid_move | integer, integer, cellT | boolean | OutOfBoundsException |
| is_winning | cellT | boolean | |
| is_any_valid_move | cellT | boolean | |
| is_game_over | | boolean | |

Semantics

State Variables

b: boardT
blacksturn: boolean

State Invariant

$\text{count}(\text{BLACK}) + \text{count}(\text{WHITE}) + \text{count}(\text{FREE}) = \text{SIZE} \times \text{SIZE}$

Assumptions

The init method is called for the abstract object before any other access routine is called for that object. The init method can be used to return the state of the game to the state of a new game.

Access Routine Semantics

init():

- transition:

$\begin{array}{c} < \text{FREE}, \text{FREE}, \text{FREE}, \text{FREE}, \text{FREE}, \text{FREE}, \text{FREE}, \text{FREE} > \\ < \text{FREE}, \text{FREE}, \text{FREE}, \text{FREE}, \text{FREE}, \text{FREE}, \text{FREE}, \text{FREE} > \\ < \text{FREE}, \text{FREE}, \text{FREE}, \text{FREE}, \text{FREE}, \text{FREE}, \text{FREE}, \text{FREE} > \\ < \text{FREE}, \text{FREE}, \text{FREE}, \text{WHITE}, \text{BLACK}, \text{FREE}, \text{FREE}, \text{FREE} > \\ \text{blacksturn}, b := \text{true}, < < \text{FREE}, \text{FREE}, \text{FREE}, \text{BLACK}, \text{WHITE}, \text{FREE}, \text{FREE}, \text{FREE} > > \\ < \text{FREE}, \text{FREE}, \text{FREE}, \text{FREE}, \text{FREE}, \text{FREE}, \text{FREE}, \text{FREE} > \\ < \text{FREE}, \text{FREE}, \text{FREE}, \text{FREE}, \text{FREE}, \text{FREE}, \text{FREE}, \text{FREE} > \\ < \text{FREE}, \text{FREE}, \text{FREE}, \text{FREE}, \text{FREE}, \text{FREE}, \text{FREE}, \text{FREE} > \end{array}$

- exception none

move(i, j, c):

- transition: $\text{blacksturn} := \neg \text{blacksturn}$ and b such that
 $\text{UpdateNS}(i, j, c, b) \wedge \text{UpdateWE}(i, j, c, b) \wedge \text{UpdateNESW}(i, j, c, b) \wedge \text{UpdateNWSE}(i, j, c, b)$
- exception $\text{exc} := (\text{InvalidPosition}(i, j) \Rightarrow \text{OutOfBoundsException} \mid \neg \text{is_valid_move}(i, j, c) \Rightarrow \text{InvalidMoveException} \mid \neg \text{is_correct_player}(\text{blacksturn}, c) \Rightarrow \text{WrongPlayerException})$

switch_turn():

- transition: $\text{blacksturn} := \neg \text{blacksturn}$
- exception $\text{exc} := (\text{is_any_valid_move}() \Rightarrow \text{ValidMoveExistsException})$

getb(i, j):

- output: $\text{out} := b[i, j]$
- exception $\text{exc} := (\text{InvalidPosition}(i, j) \Rightarrow \text{OutOfBoundsException})$

get_turn():

- output: $\text{out} := (\text{blacksturn} \Rightarrow \text{BLACK} \mid \neg \text{blacksturn} \Rightarrow \text{WHITE})$
- exception: none

count(c):

- output: $+(i, j : \mathbb{N} \mid 0 \leq i < \text{SIZE} \wedge 0 \leq j < \text{SIZE} \wedge b[i, j] = c : 1)$
- exception: none

is_valid_move(i, j, c):

- output: $out := (b[i][j] = \text{FREE}) \wedge (\text{is_validN}(i, j, c, b) \vee \text{is_validS}(i, j, c, b) \vee \text{is_validW}(i, j, c, b) \vee \text{is_validE}(i, j, c, b) \vee \text{is_validNW}(i, j, c, b) \vee \text{is_validNE}(i, j, c, b) \vee \text{is_validSW}(i, j, c, b) \vee \text{is_validSE}(i, j, c, b))$
- exception $exc := (\text{InvalidPosition}(i, j) \Rightarrow \text{OutOfBoundsException})$

is_winning(c):

- output: $out := (c = \text{BLACK} \Rightarrow \text{count}(\text{BLACK}) > \text{count}(\text{WHITE}) | c = \text{WHITE} \Rightarrow \text{count}(\text{WHITE}) > \text{count}(\text{BLACK}) | c = \text{FREE} \Rightarrow \text{false})$
- exception: none

is_any_valid_move(): *//Returns true if a valid move exists for the current player*

- output:
 $out := \exists(i, j : \mathbb{N} | 0 \leq i < \text{SIZE} \wedge 0 \leq j < \text{SIZE} \wedge b[i][j] = \text{FREE} : (\text{blacksturn} \Rightarrow \text{is_valid_move}(i, j, \text{BLACK}) | \neg \text{blacksturn} \Rightarrow \text{is_valid_move}(i, j, \text{WHITE})))$
- exception: none

is_game_over(): *//Returns true if neither player has a valid move*

- output:
 $out := \neg \exists(i, j : \mathbb{N} | 0 \leq i < \text{SIZE} \wedge 0 \leq j < \text{SIZE} \wedge b[i][j] = \text{FREE} : \text{is_valid_move}(i, j, \text{BLACK})) \wedge \neg \exists(i, j : \mathbb{N} | 0 \leq i < \text{SIZE} \wedge 0 \leq j < \text{SIZE} \wedge b[i][j] = \text{FREE} : \text{is_valid_move}(i, j, \text{WHITE}))$
- exception: none

Local Types

boardT = sequence [SIZE, SIZE] of cellT

Local Functions

UpdateNS : integer \times integer \times cellT \times boardT \rightarrow boolean

$\text{UpdateNS}(i, j, c, b) \equiv \forall(k : \mathbb{N} \mid (i - \text{CountN}(i, j, c, b)) \leq k \leq (i + \text{CountS}(i, j, c, b)) : b[k, j] = c)$

UpdateWE : integer \times integer \times cellT \times boardT \rightarrow boolean

$\text{UpdateWE}(i, j, c, b) \equiv \forall(k : \mathbb{N} \mid (j - \text{CountW}(i, j, c, b)) \leq k \leq (j + \text{CountE}(i, j, c, b)) : b[i, k] = c)$

UpdateNESW : integer \times integer \times cellT \times boardT \rightarrow boolean

$\text{UpdateNESW}(i, j, c, b) \equiv \forall(k, l : \mathbb{N} \mid (i - \text{CountNE}(i, j, c, b)) \leq k \leq (i + \text{CountSW}(i, j, c, b)) \wedge ((j - \text{CountSW}(i, j, c, b)) \leq l \leq (j + \text{CountNE}(i, j, c, b)) : b[k, l] = c)$

UpdateNWSE : integer \times integer \times cellT \times boardT \rightarrow boolean

$\text{UpdateNWSE}(i, j, c, b) \equiv \forall(k, l : \mathbb{N} \mid (i - \text{CountNW}(i, j, c, b)) \leq k \leq (i + \text{CountSE}(i, j, c, b)) \wedge ((j - \text{CountNW}(i, j, c, b)) \leq l \leq (j + \text{CountSE}(i, j, c, b)) : b[k, l] = c)$

CountN : integer \times integer \times cellT \times boardT \rightarrow integer

$\text{CountN}(i, j, c, b) \equiv$
 $\quad + (k : \mathbb{N} \mid \text{is_validN}(i, j, c, b) \wedge$
 $\quad 0 < k < i \wedge \forall(l : \mathbb{N} \mid k \leq l < i : \text{hostile}(l, j, c, b)) : 1)$

CountS : integer \times integer \times cellT \times boardT \rightarrow integer

$\text{CountS}(i, j, c, b) \equiv$
 $\quad + (k : \mathbb{N} \mid \text{is_validS}(i, j, c, b) \wedge$
 $\quad i < k < (\text{SIZE} - 1) \wedge \forall(l : \mathbb{N} \mid i < l \leq k : \text{hostile}(l, j, c, b)) : 1)$

etc.

is_validN : integer \times integer \times cellT \times boardT \rightarrow boolean

$$\text{is_validN}(i, j, c, b) \equiv \\ \exists(k : \mathbb{N} | 0 \leq k < i : \text{friendly}(k, j, c, b) \wedge \forall(l : \mathbb{N} | k < l < i : \text{hostile}(l, j, c, b)))$$

etc.

friendly: integer \times integer \times cellT \times boardT \rightarrow boolean

$$\text{friendly}(i, j, c, b) \equiv b[i, j] = c$$

hostile: integer \times integer \times cellT \times boardT \rightarrow boolean

$$\text{hostile}(i, j, c, b) \equiv (b[i, j] = \text{BLACK} \Rightarrow c = \text{WHITE} \mid b[i, j] = \text{WHITE} \Rightarrow c = \text{BLACK} \mid c = \text{FREE} \Rightarrow \text{false})$$

InvalidPosition: integer \times integer \rightarrow boolean

$$\text{InvalidPosition}(i, j) \equiv \neg((0 \leq i < \text{SIZE}) \wedge (0 \leq j < \text{SIZE}))$$

is_correctPlayer: boolean \times cellT \rightarrow boolean

$$\text{is_correctPlayer}(bt, c) \equiv (bt \Rightarrow c = \text{BLACK} \mid \neg bt \Rightarrow c = \text{WHITE})$$