

Assignment 5, Part 1, Specification

SFWR ENG 2AA4

April 6, 2017

The purpose of this software design exercise is to design, specify, implement and test a module for storing the state of an Othello game. The game board is represented as a two dimensional sequence, with the first dimension the row and the second dimension the column. The indexes are relative to the upper left hand corner of the board; that is, row 0 and column 0 are at the top left.

Othello Module

Module

Othello

Uses

N/A

Syntax

Exported Constants

SIZE = 8 *//size of the board in each direction*

Exported Types

cellT = { FREE, BLACK, WHITE }

Exported Access Programs

Routine name	In	Out	Exceptions
init			
move	integer, integer, cellT		OutOfBoundsException, InvalidMoveException, WrongPlayerException
switch_turn			ValidMoveExistsException
getb	integer, integer	cellT	OutOfBoundsException
get_turn		cellT	
count	cellT	integer	
is_valid_move	integer, integer, cellT	boolean	OutOfBoundsException
is_winning	cellT	boolean	
is_any_valid_move	cellT	boolean	
is_game_over		boolean	

Semantics

State Variables

b: boardT

blacksturn: boolean

State Invariant

$\text{count}(\text{BLACK}) + \text{count}(\text{WHITE}) + \text{count}(\text{FREE}) = \text{SIZE} \times \text{SIZE}$

Assumptions

The `init` method is called for the abstract object before any other access routine is called for that object. The `init` method can be used to return the state of the game to the state of a new game.

Access Routine Semantics

`init()`:

- transition:

< FREE, FREE, FREE, FREE, FREE, FREE, FREE, FREE >
 < FREE, FREE, FREE, FREE, FREE, FREE, FREE, FREE >
 < FREE, FREE, FREE, FREE, FREE, FREE, FREE, FREE >
blacksturn, b := true, < < FREE, FREE, FREE, WHITE, BLACK, FREE, FREE, FREE >
 < FREE, FREE, FREE, BLACK, WHITE, FREE, FREE, FREE > >
 < FREE, FREE, FREE, FREE, FREE, FREE, FREE, FREE >
 < FREE, FREE, FREE, FREE, FREE, FREE, FREE, FREE >
 < FREE, FREE, FREE, FREE, FREE, FREE, FREE, FREE >

- exception none

move(*i, j, c*):

- transition: $blacksturn := \neg blacksturn$ and *b* such that
 $UpdateNS(i, j, c, b) \wedge UpdateWE(i, j, c, b) \wedge UpdateNESW(i, j, c, b) \wedge UpdateNWSE(i, j, c, b)$
- exception $exc := (InvalidPosition(i, j) \Rightarrow OutOfBoundsException | \neg is_valid_move(i, j, c) \Rightarrow InvalidMoveException | \neg is_correctPlayer(blacksturn, c) \Rightarrow WrongPlayerException)$

switch_turn():

- transition: $blacksturn := \neg blacksturn$
- exception $exc := (is_any_valid_move() \Rightarrow ValidMoveExistsException)$

getb(*i, j*):

- output: $out := b[i, j]$
- exception $exc := (InvalidPosition(i, j) \Rightarrow OutOfBoundsException)$

get_turn():

- output: $out := (blacksturn \Rightarrow BLACK | \neg blacksturn \Rightarrow WHITE)$
- exception: none

count(*c*):

- output: $+(i, j : \mathbb{N} | 0 \leq i < SIZE \wedge 0 \leq j < SIZE \wedge b[i, j] = c : 1)$
- exception: none

is_valid_move(i, j, c):

- output: $out := (b[i][j] = \text{FREE}) \wedge (\text{is_validN}(i, j, c, b) \vee \text{is_validS}(i, j, c, b) \vee \text{is_validW}(i, j, c, b) \vee \text{is_validE}(i, j, c, b) \vee \text{is_validNW}(i, j, c, b) \vee \text{is_validNE}(i, j, c, b) \vee \text{is_validSW}(i, j, c, b) \vee \text{is_validSE}(i, j, c, b))$
- exception $exc := (\text{InvalidPosition}(i, j) \Rightarrow \text{OutOfBoundsException})$

is_winning(c):

- output: $out := (c = \text{BLACK} \Rightarrow \text{count}(\text{BLACK}) > \text{count}(\text{WHITE}) | c = \text{WHITE} \Rightarrow \text{count}(\text{WHITE}) > \text{count}(\text{BLACK}) | c = \text{FREE} \Rightarrow \text{false})$
- exception: none

is_any_valid_move(): //Returns true if a valid move exists for the current player

- output:

$$out := \exists(i, j : \mathbb{N} | 0 \leq i < \text{SIZE} \wedge 0 \leq j < \text{SIZE} \wedge b[i][j] = \text{FREE} : (\text{blacksturn} \Rightarrow \text{is_valid_move}(i, j, \text{BLACK}) | \neg \text{blacksturn} \Rightarrow \text{is_valid_move}(i, j, \text{WHITE})))$$

- exception: none

is_game_over(): //Returns true if neither player has a valid move

- output:

$$out := \neg \exists(i, j : \mathbb{N} | 0 \leq i < \text{SIZE} \wedge 0 \leq j < \text{SIZE} \wedge b[i][j] = \text{FREE} : \text{is_valid_move}(i, j, \text{BLACK})) \wedge \neg \exists(i, j : \mathbb{N} | 0 \leq i < \text{SIZE} \wedge 0 \leq j < \text{SIZE} \wedge b[i][j] = \text{FREE} : \text{is_valid_move}(i, j, \text{WHITE}))$$

- exception: none

Local Types

boardT = sequence [SIZE, SIZE] of cellT

Local Functions

UpdateNS : integer \times integer \times cellT \times boardT \rightarrow boolean

UpdateNS(i, j, c, b) $\equiv \forall(k : \mathbb{N} \mid (i - \text{CountN}(i, j, c, b)) \leq k \leq (i + \text{CountS}(i, j, c, b)) : b[k, j] = c)$

UpdateWE : integer \times integer \times cellT \times boardT \rightarrow boolean

UpdateWE(i, j, c, b) $\equiv \forall(k : \mathbb{N} \mid (j - \text{CountW}(i, j, c, b)) \leq k \leq (j + \text{CountE}(i, j, c, b)) : b[i, k] = c)$

UpdateNESW : integer \times integer \times cellT \times boardT \rightarrow boolean

UpdateNESW(i, j, c, b) $\equiv \forall(k, l : \mathbb{N} \mid (i - \text{CountNE}(i, j, c, b)) \leq k \leq (i + \text{CountSW}(i, j, c, b)) \wedge ((j - \text{CountSW}(i, j, c, b)) \leq l \leq (j + \text{CountNE}(i, j, c, b)) : b[k, l] = c)$

UpdateNWSE : integer \times integer \times cellT \times boardT \rightarrow boolean

UpdateNWSE(i, j, c, b) $\equiv \forall(k, l : \mathbb{N} \mid (i - \text{CountNW}(i, j, c, b)) \leq k \leq (i + \text{CountSE}(i, j, c, b)) \wedge ((j - \text{CountNW}(i, j, c, b)) \leq l \leq (j + \text{CountSE}(i, j, c, b)) : b[k, l] = c)$

CountN : integer \times integer \times cellT \times boardT \rightarrow integer

CountN(i, j, c, b) \equiv
+ ($k : \mathbb{N} \mid \text{is_validN}(i, j, c, b) \wedge$
 $0 < k < i \wedge \forall(l : \mathbb{N} \mid k \leq l < i : \text{hostile}(l, j, c, b)) : 1)$

CountS : integer \times integer \times cellT \times boardT \rightarrow integer

CountS(i, j, c, b) \equiv
+ ($k : \mathbb{N} \mid \text{is_validS}(i, j, c, b) \wedge$
 $i < k < (\text{SIZE} - 1) \wedge \forall(l : \mathbb{N} \mid i < l \leq k : \text{hostile}(l, j, c, b)) : 1)$

etc.

is_validN : integer \times integer \times cellT \times boardT \rightarrow boolean

$$\text{is_validN}(i, j, c, b) \equiv \\ \exists(k : \mathbb{N} | 0 \leq k < i : \text{friendly}(k, j, c, b) \wedge \forall(l : \mathbb{N} | k < l < i : \text{hostile}(l, j, c, b)))$$

etc.

friendly: integer \times integer \times cellT \times boardT \rightarrow boolean

$$\text{friendly}(i, j, c, b) \equiv b[i, j] = c$$

hostile: integer \times integer \times cellT \times boardT \rightarrow boolean

$$\text{hostile}(i, j, c, b) \equiv (b[i, j] = \text{BLACK} \Rightarrow c = \text{WHITE} \mid b[i, j] = \text{WHITE} \Rightarrow c = \text{BLACK} \mid c = \text{FREE} \Rightarrow \text{false})$$

InvalidPosition: integer \times integer \rightarrow boolean

$$\text{InvalidPosition}(i, j) \equiv \neg((0 \leq i < \text{SIZE}) \wedge (0 \leq j < \text{SIZE}))$$

is_correctPlayer: boolean \times cellT \rightarrow boolean

$$\text{is_correctPlayer}(bt, c) \equiv (bt \Rightarrow c = \text{BLACK} \mid \neg bt \Rightarrow c = \text{WHITE})$$